

### Convergence of orthonormal spline series

Let  $(t_n)_{n=2}^{\infty}$  be an arbitrary dense sequence of points in the interval  $(0,1)$  and  $t_0 = 0, t_1 = 1$ . We define  $\mathcal{S}_n$  as the space of piecewise polynomial functions of order  $k$  with grid points  $(t_j)_{j=0}^n$ , that are continuously differentiable of order  $k - 2$  at the points  $(t_j)_{j=2}^n$ . For each  $n$ , the space  $\mathcal{S}_{n-1}$  has codimension one in  $\mathcal{S}_n$  and therefore, there exists a unique function (up to sign)  $f_n \in \mathcal{S}_n$  that is orthogonal to  $\mathcal{S}_{n-1}$  and normalized in  $L^2$ . This system of functions  $(f_n)$  is called *orthonormal spline system of order  $k$  corresponding to the point sequence  $(t_n)$* . In [1] it is proved that the partial sums  $P_n f = \sum_{j=1}^n \langle f, f_j \rangle f_j$  converge a.e. with respect to Lebesgue measure to the function  $f$  and in [2] it is proved that this partial sums also converge unconditionally in  $L^p$ ,  $p \in (1, \infty)$ . In this talk, we will discuss the extension of those results to the periodic setting, [3,4].

**References.**

- [1] M. Passenbrunner and A. Shadrin: On almost everywhere convergence of orthogonal spline projections with arbitrary knots, *J. Approx. Theory* 180 (2014) 77–89.
- [2] M. Passenbrunner: Unconditionality of orthogonal spline systems in  $L^p$ , *Studia Math.* 222 (2014), no. 1, 51–86.
- [3] M. Passenbrunner: Orthogonal projectors onto spaces of periodic splines, *Journal of Complexity* 42 (2017), 85–93.
- [4] K. Keryan and M. Passenbrunner: Unconditionality of periodic orthonormal spline systems in  $L^p$ , preprint.